Impurity Spin Magnetization of Thin Fe Doped Au Films

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In order to probe the influence of the surface-induced anisotropy on the impurity spin magnetization, we measure the anomalous Hall effect in thin AuFe films at magnetic fields up to 15 T. The observed suppression of the anomalous Hall resistivity at low fields as well as the appearance of a minimum in the differential Hall resistivity at higher fields can be explained by our theoretical model, which takes into account the influence of a polycrystalline film structure on the surface-induced anisotropy. Our results imply that the apparent discrepancy between different experimental results for the size effects in dilute magnetic alloys can be linked to a different microstructure of the samples.

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In very dilute magnetic alloys, finite size effects may occur for sample dimensions comparable to the size of the Kondo screening cloud [1]. While some experiments [2] revealed a considerable decrease of the logarithmic Kondo anomaly in the resistivity of thin films and narrow wires already at the μm scale, other experiments [3] showed an almost constant Kondo anomaly for wire widths down to 40 nm. Recent theoretical calculations indicated the complex, dynamical nature of the screening cloud, implying that the simple picture of a static, spherically symmetric screening cloud is not correct [1,4].

Zawadowski *et al.* [5] linked the size dependent Kondo scattering to a surface-induced anisotropy of the magnetic impurity spins. Because of the interaction of the impurities with the conduction electrons, which suffer from the spin-orbit scattering by the nonmagnetic host atoms, the impurity spins tend to be aligned parallel to the sample boundaries [6]. The surface-induced anisotropy should remain active for more concentrated spin glass alloys. Finite size effects have indeed been observed in the resistivity of spin glasses with reduced dimensions [7,8].

Finite size effects should also be observable in the impurity spin magnetization. Earlier magnetization experiments on single film [9] and on multilayered [10] spin glasses had linked a depression of the freezing temperature T_f to a lower critical dimensionality for the spin glass transition. Here, we show that measuring the magnetic field dependence of the anomalous Hall effect in thin films of a AuFe spin glass [9] provides a powerful method to probe the influence of the surface-induced anisotropy on the Fe spin magnetization. At low magnetic fields, the magnetization signal related to the spin glass freezing is strongly suppressed when compared to the bulk behavior. The appearance of an extra magnetization signal at higher fields can be linked to a reorientation of impurity spins which are blocked by the surface-induced anisotropy at lower fields. The low field magnetization is further suppressed when

moving the Fe doping towards the film surface. We have developed a theoretical model which takes into account the polycrystalline film structure. The presence of additional internal surfaces at the grain boundaries introduces a particular spatial dependence of the spin anisotropy which is essential for understanding the Hall effect data. Our model provides an explanation for the apparent discrepancies between the different experiments which have probed the size dependence of the Kondo and spin glass resistivity.

Thin films of AuFe alloys have been prepared by codeposition on oxidized silicon wafers of Au (99.9999% purity) and Fe (99.99% purity) in an ultrahigh vacuum molecular beam epitaxy growth chamber. A multiterminal sample geometry is obtained by depositing the films through a contact mask. Apart from 30 nm thick Fe doped Au films and pure Au reference films, we have also prepared Au/AuFe/Au and AuFe/Au/AuFe trilayers. For the 30 nm thick trilayer samples, the central layer has a thickness of 15 nm, while the two outer layers have a thickness of 7.5 nm. The Hall resistance as well as the longitudinal resistance are measured with an ac resistance bridge in perpendicular magnetic fields up to 15 T.

Adding Fe impurity spins to pure Au causes the appearance of a nonlinear anomalous Hall component. Figure 1(a) shows typical Hall effect data at $T = 4.2$ K which have been obtained by McAlister and Hurd [11] for polycrystalline pure bulk Au as well as for a 0.98 at. % AuFe bulk spin glass. The anomalous Hall resistivity varies proportional to the Fe spin magnetization, and its temperature dependence at low fields reveals a sharp peak near the freezing temperature T_f . In agreement with direct magnetization measurements, the peak is washed out at higher magnetic fields [11,12].

As illustrated in Fig. 1(b), the anomalous Hall effect is much weaker in a thin 2 at. % AuFe spin glass film when compared to the bulk material. Although the Fe concentration is about twice as large as in Fig. 1(a), deviations

FIG. 1. (a) Magnetic field dependence of the Hall resistivity for a bulk polycrystalline Au sample and a bulk 0.98 at. % AuFe sample at $T = 4.2 \text{ K}$ (from Ref. [11]). (b) Magnetic field dependence of the Hall resistivity for a pure Au film and for a 2 at. % AuFe film at $T = 1 \text{ K}$. Both films have a thickness of 30 nm. For the AuFe film, the differential Hall resistivity $-d\rho_H/dB$ is also shown. (c) Magnetic field dependence of the differential Hall resistivity for the Au/AuFe/Au and AuFe/Au/AuFe trilayers (Fe concentration is 3.5 at. % for the AuFe) at $T = 1 \text{ K}$.

from the classical linear Hall resistivity of the pure Au film are very small. In order to make the nonlinear anomalous Hall component more clearly visible, we also plot in Fig. 1(b) the differential Hall resistivity $-d\rho_H/dB$. The initial variation of the differential Hall resistivity at low fields reflects the destruction of the spin glass state due to the alignment of the impurity spins. The magnetic response resulting from this alignment has been reduced by an order of magnitude when compared to the bulk material. As discussed in detail below, we can attribute the reduced amplitude of $-d\rho_H/dB$ at low fields as well as the appearance of a minimum at higher fields to the surface-induced anisotropy.

The strength of the anisotropy of an impurity spin is predicted to increase when the impurity approaches the

sample surface [5]. Consequently, the anisotropy effects should be less pronounced for a Au/AuFe/Au trilayer when compared to a AuFe/Au/AuFe trilayer. This is confirmed in Fig. 1(c) for AuFe layers with an Fe concentration of 3.5 at. %. Both samples have the same total thickness and the same Fe content. The samples also have a comparable resistivity, and the maximum in the low field ($\sim 0.01 \text{ T}$) anomalous Hall resistivity [9] occurs at a comparable temperature ($T_f \approx 5 \text{ K}$). Nevertheless, the nonlinear behavior is clearly enhanced for fields below 4 T when moving the Fe impurities away from the surface. The reduced amplitude of $-d\rho_H/dB$ for the trilayers when compared to a single AuFe film [see Fig. 1(b)] results from a shortcircuiting by the pure Au layer with a much lower resistivity.

In order to calculate the nonlinear impurity magnetization in polycrystalline AuFe films, we generalize the theory of the surface-induced anisotropy [5,6] to the case of thin films consisting of small grains. In contrast to the method used in Ref. [5], our approach, introduced in Ref. [6] for wires of dilute magnetic alloys, allows one to treat the surface-induced anisotropy in mesoscopic samples with a more complicated shape. Here, we have derived the Hamiltonian $\mathcal{H}_{\text{an}}$, which describes the surface-induced anisotropy for an impurity spin in an isolated brick-shaped grain:

$$\mathcal{H}_{\text{an}} = \mathcal{A} \sum_{\alpha, \beta} \mathcal{B}_{\alpha\beta} S_{\alpha} S_{\beta} \quad (\alpha, \beta = x, y, z). \quad (1)$$

The S_{α} are the operators for the components of the impurity spin $\mathbf{S}$. In contrast to a semi-infinite sample [5], the strength of the anisotropy has to be described in terms of a matrix with elements $\mathcal{A}\mathcal{B}_{\alpha\beta}$. Moreover, the calculated matrix elements $\mathcal{B}_{\alpha\beta}$ are complicated functions of the dimensions (a_x, a_y, a_z) of the grain and of the impurity position. The material dependent constant $\mathcal{A}$ should range between 0.01 and 1 eV for dilute AuFe alloys [5,6]. Taking the z axis parallel to the magnetic field, the magnetization of an Fe spin is given by

$$\langle S_z \rangle = -\frac{1}{2\mu_B Z} \sum_{k=1}^5 \exp\left(-\frac{\mathcal{E}_k}{k_B T}\right) \frac{d\mathcal{E}_k}{dB}, \quad (2)$$

where μ_B is the Bohr magneton, and $Z = \sum_{k=1}^5 \exp(-\mathcal{E}_k/k_B T)$. The index $k = 1, \dots, 5$ labels the roots $\mathcal{E}_k$ of the secular equation,

$$|\mathcal{H}_{S'_z S_z} - \mathcal{E} \delta_{S'_z S_z}| = 0 \quad (S_z, S'_z = -2, -1, 0, 1, 2), \quad (3)$$

with the Hamiltonian $\mathcal{H} = -2\mu_B S_z B + \mathcal{H}_{\text{an}}$.

In Fig. 2 the calculated differential magnetization $[d\langle S_z \rangle / dB]_{\text{gr}}$ (the square brackets with subscript "gr" correspond to an average over impurity positions within a grain) is shown as a function of the magnetic field for different lateral dimensions of the grains. The height a_z of the grains is fixed at 30 nm, i.e., the thickness of the AuFe film shown in Fig. 1(b). In the limiting case

FIG. 2. Calculated magnetic field dependence of the differential magnetization $[d\langle S_z \rangle / dB]_{gr}$ for grains with height $a_z = 30$ nm and lateral dimensions $a_x = a_y = a$. Inset: Spatial distribution of the differential magnetization for a cross section perpendicular to the magnetic field at the center of a grain with $a = 50$ nm.

of a *single-crystal film* ($a_x, a_y \rightarrow \infty$), the impurity spin states at $B = 0$ are known [5] to be the eigenstates of S_z , the energy eigenvalues being proportional to S_z^2 . At low temperatures, only the state with $S_z = 0$ will be populated. Hence, the impurity spin does not respond to a weak magnetic field. With increasing B the energy level with $S_z = 1$ becomes lower than that with $S_z = 0$. This gives rise to the first peak in the field dependence of $[d\langle S_z \rangle / dB]_{gr}$. The second peak appears when the state with $S_z = 2$ becomes the ground state. The theoretical result for the single-crystal film in Fig. 2 clearly fails to describe our experimental results, since the calculated impurity spin magnetization remains zero at low magnetic fields (all spins are blocked parallel to the surface).

In Ref. [6], it was already shown that in narrow wires the presence of differently oriented surfaces leads to a rather intricate behavior of the impurity-spin anisotropy when compared to the case of a film. In *brick-shaped grains*, the competing influence of mutually perpendicular surfaces on the magnetic anisotropy gives rise to a partial cancellation of the anisotropy effect, resulting in a shift of the peaks in $[d\langle S_z \rangle / dB]_{gr}$ towards lower fields. Moreover, there exist specific locations within the grains where the magnetic anisotropy energy becomes negligibly small. At these locations the bulk behavior of the impurity spins is restored. Hence, a limited number of spins contribute to the spin glass freezing and are sensitive to very weak magnetic fields. In the inset of Fig. 2, we illustrate the large difference in the predicted response of spins located near the corners of the grains when compared to spins located more towards the center of the grains. For grains with lateral

sizes larger than (but still comparable to) the height, our theoretical model predicts that a minimum in $[d\langle S_z \rangle / dB]_{gr}$ can appear at relatively small magnetic fields. For those grains the initial part of the theoretical curves is similar to the measured differential Hall resistivity shown in Figs. 1(b) and 1(c). The aforementioned nonmonotonous behavior gradually disappears both in our experiments and in our theoretical model at temperatures well above the measured freezing temperature T_f . A consistent description of our anomalous Hall data requires one to assume a large value $\mathcal{A} = 0.12$ eV in Eq. (1). This implies that a larger fraction of the alignment of the Fe spins by the magnetic field occurs at extremely high fields which are not accessible in the experiment.

Figure 3(a) shows the calculated field dependence of an average $[d\langle S_z \rangle / dB]_{cs}$ over the positions of the impurities located within a cross section of a grain perpendicular to the magnetic field. The different curves correspond

FIG. 3. (a) Calculated magnetic field dependence of the differential magnetization $[d\langle S_z \rangle / dB]_{cs}$ for a grain after averaging over a cross section perpendicular to the magnetic field. Different curves are for different distances Δz to the top or bottom of the grain with a height of 30 nm and lateral size of 50 nm. (b) Comparison between the differential Hall resistivity $-d\rho_H/dB$ measured for the Au/AuFe/Au trilayer (solid curve) and the calculated differential magnetization $[d\langle S_z \rangle / dB]_{gr}$ for an ensemble of Au/AuFe/Au grains with a height of 30 nm and a thickness of the central AuFe layer of 15 nm (dashed curve). For the lateral grain size a , a lognormal distribution is assumed (see text). The inset shows an STM image of the surface of the Au/AuFe/Au trilayer.

to different distances Δz from the cross section to the top (or bottom) of the grain. The theoretical curves can be compared to the experimental field dependence of $-d\rho_H/dB$ for the Au/AuFe/Au and the AuFe/Au/AuFe trilayer shown in Fig. 1(c). The low field variation is much weaker for the AuFe/Au/AuFe trilayer. This is in agreement with our theoretical result that the surface-induced anisotropy becomes stronger for Fe spins which are closer to the top (or bottom) of a grain.

The inset of Fig. 3(b) shows a scanning tunneling microscopy (STM) image of the surface of the Au/AuFe/Au sample, revealing a rather broad distribution of grain sizes. In order to quantitatively fit the experimental data, we therefore calculate the magnetization for an ensemble of grains of different lateral size a , distributed lognormally with a statistical median $\bar{a}$ and a standard deviation σ . In Fig. 3(b), the measured differential Hall resistivity $-d\rho_H/dB$ for the Au/AuFe/Au trilayer is compared to the field dependence of $[d\langle S_z \rangle/dB]_{gr}$, calculated for an ensemble of Au/AuFe/Au grains with $\bar{a} = 80$ nm and $\sigma = 1.5$. We note that the value of 80 nm is larger than the typical grain size inferred from the STM images (20 nm). Our theoretical approach with isolated grains is strictly valid only when elastic defect scattering at the grain boundaries fully destroys the anisotropy which is caused by the conduction-electron-mediated interaction of an Fe spin with host atoms from neighboring grains. Using a larger grain size for the calculations allows one to take into account that a fraction of the electrons still moves ballistically between adjacent grains.

We conclude that our theoretical model for the surface-induced anisotropy of magnetic impurities in small metallic grains allows a quantitative description of the anomalous Hall resistivity in polycrystalline AuFe spin glass films. The small impurity spin magnetization at low magnetic field also provides an explanation for the small amplitude of the spin glass resistivity in thin AuFe films [8]. It is clear that the surface-induced anisotropy strongly affects the spin glass freezing, implying that the analysis of previous measurements, which investigated the reduction of the freezing temperature T_f in thin films [9] and multilayers [10], should be revised. At this point it is not yet clear to what extent the observed effects are caused by an intrinsic size effect or if they can be totally accounted for by the surface-induced anisotropy.

For Kondo alloys with a small impurity content (~ 100 ppm), we are no longer able to measure the anomalous Hall effect. The surface-induced anisotropy should still cause a reduction of the impurity spin magnetization, resulting in a suppression of the Kondo resistivity. Earlier measurements of the Kondo resistivity in AuFe films confirmed the presence of such a suppression, which became weaker when covering the films with a pure Au layer [13]. Since the surface-induced blocking of a magnetic impurity spin is sensitive to the specific polycrystalline sample structure, the apparent discrepancy between different experimental results [2,3,13] for the

size dependence of the Kondo resistivity can be linked to a different microstructure of the samples.

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